





## Radiotherapy Treatment Planning

The Role of Operations Research and Multidisciplinary Collaboration



# OR impacts the world everyday













### OR impacts HEALTH



Kluwer's International Series



ADVANCING THE STATE-OF-THE-ART

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OPERATIONS RESEARCH AND HEALTH CARE

A Handbook of Methods and Applications

edited by Margaret L. Brandeau François Sainfort William P. Pierskalla Health operations management

Public Policy and Economic Analysis

**Clinical Applications** 

## 29

RADIOTHERAPY TREATMENT DESIGN AND LINEAR PROGRAMMING

Allen Holder

#### **30** OPTIMIZATION TOOLS FOR RADIATION TREATMENT PLANNING IN MATLAB

Michael C. Ferris<sup>1</sup>, Jinho Lim<sup>2</sup> and David M. Shepard<sup>3</sup>

### Radiotherapy

- Used for cancer patients, with curatintent
- At least 50% of all the cancer patients will submitted to radiotherapy treatments
- In Europe alone, near 2 million patients are treated per year
- There are different treatment modalities:
  - Intensity Modulated Radiation Therapy (IMRT)
  - Volumetric Modulated Arc Therapy (VMAT)
  - Protons
  - Brachytherapy
  - ...

OR impacts every patient, because OR is in the core of radiotherapy treatment planning!











What are the angles/arcs that should be used? What should be the patient couch position? +

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# Problem description



What should be the radiation intensities (fluence maps)?



What should be the leaf sequencing? How should the leaves move so that the desired fluence maps are obtained?



## Treatment planning



## **Objective:** achieving fully automated radiotherapy treatment plans





The quality is highly dependent on the planner's time availability and experience.



# Medical prescription

- Doses that should be delivered to the volumes to treat (PTV –Planning Target Volume)
- Dose limits for the OARs organs at risk

Structure	Type of constraint		Limit
Spinal cord	Maximum dose	Lower than	45 Gy
Brainstem	Maximum dose	Lower than	54 Gy
Left parotid	Mean dose	Lower than	26 Gy
Right parotid	Mean dose	Lower than	26 Gy
$\mathrm{PTV}_{70}$	D <sub>95%</sub>	Greater than	66.5 Gy
$\mathrm{PTV}_{70}$	Maximum dose	Lower than	74.9 Gy
PTV <sub>59</sub>	D <sub>95%</sub>	Greater than	56.4 Gy
PTV 59	V <sub>107%</sub>	Lower than	Percentage of PTV <sub>70</sub> volume inside PTV <sub>59</sub> plus a 10% margin
Body	Maximum dose	Lower than	80 Gy







#### Treatment Planning System

- Mathematical Optimisation
- Dose computation



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## Optimal or admissible? Inverse Optimisation!

- We know what we want to achieve: compliance with the medical prescription.
- We are unsure of the path to reach this goal.
- Therefore, we are seeking an admissible solution for a highly constrained problem, but...
- If possible, we aim to exceed the established constraints!



We are thrilled!! We were able to improve the value of our objective function around 10%!!!



Non-linearities in constraints and objectives.

Several and conflicting objectives.

Uncertainties: robust optimization.

Very large problems, very large matrixes.

Allthe ingredients for a very difficult problem











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## OR toolbox

- Mathematical Modelling
- Exact optimization approaches
- Heuristics/Metaheuristics
- Simulation
- Statistics

• ...

• Machine Learning

CEJOR (2014) 22:431–455 DOI 10.1007/s10100-013-0289-4

ORIGINAL PAPER

#### A genetic algorithm with neural network fitness function evaluation for IMRT beam angle optimization

Joana Dias · Humberto Rocha · Brígida Ferreira · Maria do Carmo Lopes

## Machine Learning WStbR? OR!

Neural networks can be used as function approximators when dealing with expensive objective functions



Machine learning can make optimization algorithms run faster (parameter optimization, initial solution...).



Machine learning can help in the algorithmic choice.



What are the angles/arcs that should be used? What should be the patient couch position?

# Problem description



What should be the radiation intensities (fluence maps)?



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#### Fluence Map Optimisation

$$f(w) = Min_w \sum_{i=1}^{V} \left[ \frac{\lambda_i}{L_i} \left( L_i - \sum_{j=1}^{N} D_{ij} w_j \right)_+^2 + \overline{\lambda_i} \left( \sum_{j=1}^{N} D_{ij} w_j - U_i \right)_+^2 \right]$$

- Minimise the squared deviations from the desired dosimetric values for each structure of volume.
- A considerable number of parameters that must be tuned.

# MEDICAL PHYSICS

The International Journal of Medical Physics Research and Practice

Therapeutic interventions

#### Automated fluence map optimization based on fuzzy info systems

Joana Dias, Humberto Rocha, Tiago Ventura, Brígida Ferreira, Maria do Carmo Lopes

First published: 05 February 2016 | https://doi.org/10.1118/1.4941007

## Fluence Map Optimization



Quadratic Programming Optimization Problem



#### Fuzzy Inference Systems

## Fluence Map Optimization



Quadratic Programming Optimization Problem



#### **Fuzzy Inference Systems**



Reinforcement learning to learn the best fuzzy rules



## Reinforcement Learning ~Classical conditioning theory





Q-table	Action 1	Action 2
State 1		
State 2		
State 3		



- 1. The structure is complying with the medical prescription.
- 2. The structure is not respecting dose constraints by less than 10%.
- 3. The structure is not respecting dose constraints by more than 10%.

EXISTING STATES

1. Use fuzzy rules defined by set 1 to change the parameters of the FMO model.

POSSIBLE ACTIONS

2. Use fuzzy rules defined by set 2 to change the parameters of the FMO model.



**Results:** Our original approach had already proven to be able to obtain high quality treatment plans.

WITH THE INCLUSION OF Q-LEARNING, FUZZY RULES ARE DYNAMICALLY CHANGED AS THE ALGORITHM PROGRESSES, INSTEAD OF BEING FIXED.

This has led to a decrease in the total number of iterations needed to reach a treatment plan complying with the medical prescription.

Average values considering Cross Validation show a reduction in the total number of iterations ranging from 50% to 63%.

**Conclusion**: Automated treatment planning can be achieved by combining ML with optimization models and algorithms.

In this work an ensemble approach joining RL, optimization and fuzzy inference systems is presented for fully automated treatment planning WITHOUT RESORTING TO LARGE TRAINING DATASETS.



Reinforcement learning, as well as other ML approaches, can be naturally integrated with OR models and methods.



Difficult and interdisciplinary real world problems will gain with the integrated use of different tools.



Machine learning is just one more tool that Operations Researchers can/should use. It is not the holy grail for all existing problems.



So many new avenues for research and for tackling real world problems!

Operations Research and multidisciplinary collaboration in real world applications



Have an open mind and be willing to learn.



Step into the others' shoes and understand other points of view.



Understand what is really important: what will be the results that can make the difference.



Incorporate existing knowledge into OR way of thinking.



Be flexible and use the most adequate tools.



### **Radiotherapy Treatment Planning**

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