Or on OR

Martin Grötschel

20th European Conference on Operational Research EURO XX, Rhodes, Greece July 7, 2004



Institute of Mathematics, Technische Universität Berlin (TU	JB)
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- DFG-Research Center "Mathematics for key technologies" (FZT 86)
- Konrad-Zuse-Zentrum f
 ür Informationstechnik Berlin (ZIB)

Martin Grötschel

http://www.zib.de/groetschel

- 1. Introduction
 - Where am I from?
 - Selecting a title
 - Revealing a secret
- 2. What is OR? (A name is a name, or not?)
- 3. OR on OR
- 4. Answering the HARD questions
 - What can we do? Examples:
 - Linear and integer programming
 - Public transportation
 - Telecommunication
 - What should we look at?
- 5. What is good OR?

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Konrad-Zuse-Zentrum für Informationstechnik Zuse-Institute Berlin (ZIB)











Berlin University of Technology

Main - Campus

Mathematics

Brandenburg Gate

- 32 22 24 24 24 2

APPER

The DFG Research Center in Berlin

supported by the German National Science Foundation













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Former Lecture/ Article Titles of EURO Gold Medal Winners

- Egon Balas: "Some thoughts on the development of integer programming during my research career" (2001)
- Rainer E. Burkard: "OR Utopia" (1997)
- Jan Karel Lenstra: "Whizzkids" (1997)
- Pierre Hansen: "A short discussion of the OR crisis" (1986)
- Dominique de Werra: "What is my objective function?" (1995)
- My mulitcriteria optimization goal:
 - Minimize the title length
 - Use as few letters as possible
 - The title should have a meaning

"Or on OR"

6 letters, 3 different letters

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Claude Berge EURO Gold Medal 1989



Claude passed away on June 30, 2002

This week, a memorial conference is held in Paris



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A Childhood Dream

- I start with telling you a se revealed to anybody before
- As a child I dreamt of becc at the Olympic Games.
- I was quite good in shot pr





A Childhood Dream

- I start with telling you a secret that I never revealed to anybody before.
- As a child I dreamt of becoming a gold medalist at the Olympic Games.
- I was quite good in shot put.
- I just was not good enough (#9 in Germany) and did not make the 1972 German olympic team.
- Receiving an EURO Gold Medal in Greece is the second best that could have happened to me.

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Operational Research

- S. Vajda, (article on EURO Gold Medal Ceremony) "The three ages of Operational Research", European Journal of Operational Research 45(1990)131-134
 - "I believe that the term fits awkwardly those activities which OR comprises now, but it is too late to change."
- R. L. Ackoff, "The future of Operational Research is past" Journal of the Operational Society 30(1979)93-104
- J. Krarup, "EURO Gold Medal 1986: A parable on twolevel parallelism",
 - European Journal of Operational Research 38(1989)274-276
 - "...an interdisciplinary bastard like operational research ... "

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Google Search (Saturday morning)

- "operations research" about 929,000 hits for "operations research"
- "operational research" about 226,000 hits for "operational research"
- "Unternehmensforschung" about 9,660 hits for "Unternehmensforschung"
- "Unternehmungsforschung" about 83 hits for "Unternehmungsforschung"
- "Operationsforschung"

about **719** hits for **"Operationsforschung"** (Mostly from medicine, though)

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- Introduction
 - Where am I from?
 - Selecting a title
 - Revealing a secret
- What is OR? (A name is a name, or not?)
- OR on OR
- Answering THE hard questions
 - What can we do? Examples:
 - Linear and integer programming
 - Public transportation
 - Telecommunication
 - What should we look at?

• What is good OR?

The basic questions of philosophy

- Where do we come from?
- Who are we?
- Where are we going to?
- What is the meaning of life?



The basic questions of an OR consultant

- I made a long list, but deleted it yesterday since
 I thought that you would know that anyway.
- (I will try not to bore you too much.)



Operational Research: approaching it as a subject

- OR as a topic in mathematics
 - optimization

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- mathematical programming
- OR as a topic in management science
 - operations management, business information management
 - management engineering
- OR as a topic in engineering
 - industrial engineering
 - supply chain management/flexible manufacturing
- OR as a topic in computer science
- OR as a topic in psychology/sociology
- Systems Theory/Cybernetics

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. . .

Decision Sciences, Decision Aid

de Werra's sweep

D. de Werra: "What is my objective function?"

European Journal of Operational Research 99(1997)207-219

- 2. OR is a pure science
- 3. OR is an open science
- 4. OR relies on basic sciences and on life sciences
- 5. OR is a natural science
- 6. OR is an art
- 7. OR does miracles



Dominique forgot: OR is an applied science

Academic OR in Berlin

- Technische Universität Berlin
 - Fakultät IV Elektrotechnik und Informatik
 - Institut f
 ür Wirtschaftsinformatik und Quantitative Methoden
 - Operations Research (OR)
 - Fakultät VIII Wirtschaft und Management
 - Fachgebiet Produktionsmanagement
 - Fakultät II Mathematik und Naturwissenschaften
 - Institut f
 ür Mathematik
 - Arbeitsgruppe Algorithmische und Diskrete Mathematik M. Grötschel
 - Freie Universität Berlin

- Fachbereich Wirtschaftswissenschaft
 - Institut f
 ür Produktion, Wirtschaftsinformatik und OR
- Humboldt Universität Berlin
 - Wirtschaftswissenschaftliche Fakultät
 - Institut für Operations Research

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Answering the HARD questions

• What do I mean?

I think that OR should start adressing politically relevant "global questions" seriously.

• After a few examples I will be more precise.



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Typical optimization problems

$$\max f(x) \text{ or } \min f(x)$$
$$g_i(x) = 0, \quad i = 1, 2, ..., k$$
$$h_j(x) \le 0, \quad j = 1, 2, ..., m$$
$$x \in \mathbf{R}^n \text{ (and } x \in S)$$

$\min c^T x$	$\min c^T x$
Ax = a	Ax = a
$Bx \leq b$	$Bx \le b$
$x \ge 0$	$x \ge 0$
$(x \in \mathbf{R}^{n^{\mathbf{n}}})$	$x_i \in \mathbb{Z}$ for some i
$(x \in \mathbf{k}^{n^{\mathbf{n}}})$	$(x_i \in \{0,1\} \text{ for some } i)$

"general" (nonlinear) program NLP

linear program LP

(linear) (mixed-) integer program IP, MIP

program = optimization problem



Special "simple" combinatorial optimization problems

Finding a

- minimum spanning tree
- shortest path
- maximum matching
- maximal flow through a network
- cost-minimal flow



solvable in polynomial time (and very fast in practice)

Special "hard" combinatorial optimization problems

- travelling salesman problem
- Iocation und routing
- set-packing, partitioning, -covering
- max-cut
- Inear ordering
- scheduling (with a few easy exceptions)
- node and edge colouring



NP-hard (in the sense of complexity theory)

The most successful solution techniques employ linear programming as a bounding procedure.

by courtesy of Bob Bixby

LP Progress: 1988 – 2000

Algorithms

Primal simplex in 1988 *versus* Best(primal,dual,Barrier) today 2360x

- Machines
 - 800x
- Net: Algorithm * Machine ~ 1 900 000x



Linear Programming 1987-2000

- "A Model that might have taken a year to solve 10 years ago, can now solve in less than 10 seconds."
- Machine

old machine	new machine	Speedup
Sun 3/50	Pentium 4, 1.7 GHz	800
Sun 3/50	Compaq Server ES 40, 667 MHz	900
Intel 386, 25 MHz	Compaq Server ES 40, 667 MHz	400
IBM 3090/108S	Compaq Server ES 40, 667 MHz	45
Cray X-MP/416	Compaq Server ES 40, 667 MHz	10

Mathematics

old code	new code	Estimated Speedup
XMP	Oplex 1.0	4,7
Cplex 1.0	Oplex 5.0	22,0
Cplex 5.0	Oplex 7.1	3,7
XMP	Oplex 7.1	960

Robert E. Bixby, Solving Real-World Linear Programs: A Decade and More of Progress. Operations Research 50 (2002)3-15.



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Progress in Integer Programming



This book appeared just two weeks ago.

One particularly interesting article on MIP:

Mixed-Integer Programming: A Progress Report			
Robert	E. Bixby, Mary Fenelon, Zonghao Gu, Ed Rothberg, and		
Roland	Wunderling	309	
18.1	Linear Programming	309	
18.2	Mixed-Integer Programming	313	
18.3	A Short Computational History of Mixed-Integer Programming	315	
18.4	The New Generation of Codes	317	
18.5	Computational Results	320	
Bibliog	raphy	323	

Bixby et al.: LP Speedups

Table 18.2. Speedups—1988 to 2002.

Algorithm

Simplex algorithms 960 Simplex and barrier algorithms 2360 Machines

Simplex algorithms800Barrier algorithms13000



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Bixby et al.: Opinion

Top computational advances during the last 15 years:

- robust dual simplex algorithms;
- linear algebra improvements;
- interior-point algorithms;
- automatic problem simplification ("presolve").



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Bixby et al.: New MIP features

New features of the new generation of mixed-integer programming codes

- linear programming: stable, robust, dual simplex algorithms;
- variable/node selection: probing on dives, strong branching;
- primal heuristics: multiple heuristics applied within the search tree;
- node presolve: fast, incremental bound strengthening;
- presolve: probing in constraints;



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Bixby et al.: MIP instances

Hard test cases:

- total models in test: 978;
- solved to optimality:
 - CPLEX 5.0: 569 (58%),
 - CPLEX 8.0: 755 (77%);
- among those not solved to optimality with CPLEX 8.0:
 - 116 had gap less than 10% (11.9%),
 - 32 had no integral solution (3.2%);
- using CPLEX 8.0 and "MIP emphasis feasibility" on the 32 models with no feasible solution:
 - 25 found no feasible solution (2.6%).

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Bixby et al.: MIP Speedups

Table 18.4. Speedups for solvable models.

No.	CPLEX 5.0 time	Geometric
models	(seconds)	mean
758	> 0	12
551	> 1	33
463	> 10	59
375	> 100	97
294	> 1000	191
229	> 10000	357
189	>100000	528



Bixby et al.: Improvement factors

Table 18.5. CPLEX 8.0–effects of individual features.

Feature	Degradation
No cuts	53.7
No presolve	10.8
CPLEX 5.0 presolve	3.1
CPLEX 5.0 variable selection	2.9
No heuristics	1.4
No node presolve	1.3
No probing on dives	1.1


Bixby et al.: Which cuts work?

 Table 18.6. CPLEX 8.0–effects of individual cuts.

Cut type	Factor
Gomory mixed-integer	2.52
MIR	1.83
Knapsack cover	1.40
Flow cover	1.22
Implied bound	1.19
Path	1.04
Clique	1.02
GUB cover	1.02
Disjunctive	0.53



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The "classical" Transportation Problem in Mathematical Programming





$$\sum_{j \in T} x_{ij} = a_i \quad \forall i \in S$$

$$\sum_{i \in S} x_{ij} = b_j \quad \forall j \in T$$

 $0 \le x_{ii} (\le cap_{ii})$

- This problem rarely occurs in real life in its pure form.
- It does appear as a subproblem of some much more complex real problems.
- It can be solved very quickly.

T = sinks, destinations, demand

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High Quality Public Transportation: Mathematical, Social, Political, and Business Aspects

My research group at ZIB has, for more than a decade, worked on various mathematical aspects of public transportation.

- We have optimized the transport of disabled people in Berlin,
- found the minimal number of busses to run the Berlin and other city or regional bus systems,
- solved driver scheduling problems and



many other optimization problems of this type.

High Quality Public Transportation: Mathematical, Social, Political, and Business Aspects

These problems are, in general, of very large scale and represent significant mathematical challenges. I will sketch some of the achievements briefly in my talk.

It turned out, though, that implementing solutions of such problems often creates (unexpected) social or polititical difficulties.



This is an example of a HARD question.

High Quality Public Transportation: Mathematical, Social, Political, and Business Aspects

But what is a "good" public transportation system?

Can such a system result from deregulation? How does one deregulate, e.g., the railway system of a country, properly?



We are currently investigating such and related issues which are highly relevant for everybody's everyday life. There are more questions than answers.

Examples of practically important and challenging transportation problems

Some of the tasks that have to be addressed:

- planning routes
- assigning vehicles
- dispatching drivers
- improving quality
- informing customers
- creating (multi-modal) links
- controlling fleets
- coordinating tours
- keeping track of jobs
- optimizing schedules
- Iocating vehicles





film produced by IVU

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The ZI B Transportation Team, including former members

Public Transport: Ralf Borndörfer Fridolin Klostermeier Christian Küttner Andreas Löbel Sascha Lukac Marc Pfetsch

Steffen Weider

Online Transportation:

Norbert Ascheuer

Sven O. Krumke

Diana Poensgen

Jörg Rambau

Luis Miguel Torres

Andreas Tuchscherer

Tjark Vredeveld

Grötsche

The ZI B Transportation Team spin-off companies

Intranetz:



LBW:

Ralf Borndörfer

Andreas Löbel

Steffen Weider



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Service vehicle planning at ADAC



41 ADAC DADAC PANNE

Supereinsatz. In Berlin und Brandenburg mussten die Gelben Engel letztes Jahr mehr als 240 000 Mal ausrücken, um Havaristen in der Hauptstadt und auf 1700 Autobahnkilometern wieder flottzumachen – ein Rekordeinsatz. Einen Rückgang von zehn Prozent bei den Pannen registrierten dagegen die Gelben Engel in Mecklenburg-Vorpommern. Bei insgesamt 72 389 Einsätzen schafften sie jedoch auch einen Rekord: In 84 Prozent der Fälle konnten die Autofahrer mit dem Wagen weiterfahren. Martin

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"Unit" of the service fleet: Yellow Angel

gelber Engel

1,700 yellow angels

10,000 calls per day

Online aspects at ADAC



- Requests are not known in advance
- Decisions are based on incomplete information
- Suboptimal results
- How to evaluate an online algorithm?

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Yellow Angels

- A prototype of our dispatching software is in use at two of the five ADAC dispatching centers in Germany.
- considerable planning improvement reached
- in full use everywhere in Germany probably at the end of this year



Telebus: Transportation of disabled people



The "Telebus mathematics"

Finding a "Good" Mathematical Model

Tourengenerierung



Ermittlung von möglichen Anschlußfahrten

Ort



Zeit

 Vor der eigentlichen Tourenplanung werden Fahraufträge zu Bestellungen verknüpft.

 Z.B. Zielsammelfahrt (I: 1, 2), Einbindung (II: 3, 4), Startsammelfahrt (III: 5, 6, 7),

Anbindung (IV: 8, 9), Mehrfachanbindung (V: 10, 11, 12).

Ziel: Minimierung der Besetztkilometer

Die Verknüpfungsoptimierung

Finding a "Solvable" mathematical model: Set Partitioninging

Solution technology

We employ: • various heuristics:

- clustering TSP/ Routing improvement
- cutting planes based on the set packing and set covering polytopes
- column generation to dynamically
 - generate "good" tours/variables

branch&cut

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Set Partitioning

Ganzzahlige Programmierung: Set-Partitioning-Modell

 $\min c^{T} x$ Ax = 1 $x \ge 0$ where A is a 0/1-matrix



Polyedrische Kombinatorik: Cliquenungleichung

Where is the mathematics?

Improvements

We employ:

- various heuristics: clustering TSP/ Routing improvement
- cutting planes based on the set packing and set covering polytopes

column generation

to dynamically generate "good" tours/variables

branch&cut

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Ergebnisse

- Serviceverbesserung
- Kostenreduktion
- Vereinfachung der Arbeitsabläufe
- Telebus-Computersystem







Some Telebus stories

- History: The system, newspaper reporter
- Social and political context (Berlin, BMBF)
- Industry interests (subsidies)
- Riding telebuses, psychology of customers
- Taxi and "social" transport companies
- union influence
- psychology of employees and bus companies



Testimony in Berlin House of Representatives

Planning Public Transportation

Phase:	Planning	Scheduling	Dispatching	
Horizon:	Long Term	Medium term Timetable Period	(very) Short term Day of Operation online planning	
Objective:	Service Level	Cost Reduction	Get it done	
Steps:	Network Design Line Planning Timetabling	Vehicle Scheduling Duty Scheduling Duty Rostering	Crew Assignment Delay Management Failure Management	



Martin Grötschel **Public Transport Planning**

Cost Coverage **Fare Prices Construction Costs** Network Topology **Travel Times** Lines Service Frequency Frequencies **Connections** Timetable Sensitivity Vehicle Rotations **Relief Points Duties Duty Mix Rosters** Fairness Crew Assignment Service Disruptions **Operations** Control

Company wide Departments Several Depots Depots Interlining Line Groups Several Lines Lines Vehicle Rotations Vehicle Rotations



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Projects



Partners



A HARD Question

What is a "good" public transportation network?



Network Planning: A didactical example city



Origin/ Destination Matrix for the didactical example

	Ι	Π	III	IV	V	VI
Ι	1500	0	2000	0	1000	500
Π	500	0	3000	0	0	500
III	500	0	0	0	0	500
IV	1000	0	3000	0	500	500
V	2000	0	2000	0	500	500
VI	1000	0	1000	0	500	500



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A real Origin/ Destination-Matrix: Potsdam





Potsdam

Network Planning: available streets/ tracks



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MIP Model for Network Planning

Variables: $y_p \in \mathbf{R}_+$ passenger flow on path $p \in P_{st}$ $z_a \in \{0,1\}$ use track/street a



s.t.

$$\sum_{a} \gamma_{a} z_{a} + \sum_{p} \tau_{p} y_{p}$$
$$\sum_{p \in P_{st}} y_{p} = d_{st}$$
$$\sum_{p:a \in p} y_{p} \leq u_{a} z_{a}$$

getting the data adequate modelling

 $\forall s,t$ transport all passengers

$$\forall a$$
 capacity constraints





Network Planning: selected network of streets and tracks



Network Planning: The Potsdam Tram Network



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Line Planning: our didactical example city



MIP Model for Line Planning

Variables:
$$y_p \in \mathbf{R}_+$$
passenger flow on path $p \in P_{st}$ $x_\ell \in \{0,1\}$ choose line ℓ \uparrow $f_\ell \in \mathbf{R}_+$ frequency of line ℓ huge number of variables

$$\min \sum_{\ell} (C_{\ell} x_{\ell} + c_{\ell} f_{\ell}) + \sum_{p} \tau_{p} y_{p}$$

$$s.t. \qquad \sum_{p \in P_{st}} y_{p} = d_{st} \qquad \forall s,t$$

$$\sum_{p:a \in p} y_{p} \leq \sum_{\ell:a \in \ell} \kappa_{\ell} f_{\ell} \qquad \forall a$$

$$f_{\ell} \leq F x_{\ell} \qquad \forall \ell$$

. . .

 $\forall s,t$ transport all passengers

- $\forall a$ capacity constraints
- ✓ℓ frequency bounds other linear constraints

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The currently existing Potsdam Network of Lines







- S-Bahn
- regional train



Network of all Public Transportation Lines in Potsdam



New Lines in Potsdam



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Passenger Flow in the new Potsdam Network of Lines



Planning prices and frequencies

- Ansatz
 - "Controlling" demand via prices and travel times
 - Price system = Individual price + ???
 - Maximize profit
 - Electronic Ticketing
- Status
 - Research project
 - Data?
 - Mathematical models ?
 - Giant amount of literature on topics of questionable value for practice (versions of local elasticities)

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Planning frequencies & synchronized timetables







a code developed at ZIB, maintained and distributed by spin-off company

LBW GbR (Löbel, Borndörfer & Weider)

Mathematical Model and Algorithmic Approach:

ZIE Martin Grötschel Multicommodity Flow model solved by Lagrangean relaxation and dynamic column generation

IP Model for Vehicle Scheduling

$$\min \sum_{d \in D} \sum_{ij \in A^d} c_{ij}^d x_{ij}^d$$

$$\sum_{d \in D} \sum_{tj \in A^d} x_{tj}^d = 1 \quad \forall t \in T \quad (Flow Requ.)$$

$$\sum_{d \in D} \sum_{tj \in A^d} x_{tj}^d - \sum_{d \in D} \sum_{it \in A^d} x_{it}^d = 0 \quad \forall t \in T, d \in D \quad (Flow Cons.)$$

$$\sum_{dt \in A^d} x_{dt}^d \leq \kappa_d \quad \forall d \in D \quad (Capacities)$$

$$x \in \mathbf{Z}_+^A \quad (Integrality)$$



- D Depots
- T Timetabled Trips

vehicle utilization



ZR

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several vehicle schedules



ZR

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VS-OPT employed in Berlin (BVG)

- Real Really Large-Scale Optimization
 - 28.000 scheduled trips (worldwide largest known instance)
 - 100 million degrees of freedom (of 400 mio possible)
 - optimization of a whole transportation company
 - no heuristic simplifications
 - "Lagrangean Pricing"-technique
- Mathematical quality guarantee
 - fleet minimal solution
 - at most 1% off minimal cost
- Added value
 - Scenario analysis
 - Sensitivity analysis
 - Stability, Fixing, Freezing, Outsourcing, etc.
- Running time
 - Minutes on standard PCs

In other words, we have a multicommodity flow problem with 100 million integer variables and can solve it in a few minutes on a laptop

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Mathematical duty scheduling DS-OPT



- Types of duties
 - Investigating whole paths
 - supplementary duty elements
- 2.000 duty elements:
 - 50.000 nodes
 - 280.000 links (edges)
 - ∞ duties

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IP Model for Duty Scheduling

$$\min \sum_{j \in J} c_j x_j + \sum_{b \in B} p_b^+ s_b^+ + \sum_{b \in B} p_b^- s_b^-$$

$$\sum_{j \in J} a_{ij} x_j = 1 \quad \forall i \in I \quad \text{(Tasks)}$$

$$\sum_{b \in B} d_{bj} x_j + s_b^+ - s_b^- = d_b \quad \forall b \in B \quad \text{(Mix)}$$

$$x \in \{0,1\}^J \quad \text{(Integrality)}$$

I – Tasks

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B – Mix (Base) Constraints

DS-OPT

- Lagrangean Shortest Path Pricing
 - Linear Resource Constraints
 - Resource Constrained Shortest Path Model
 - Lagrange Relaxation of Linear Constraints
 - Shortest Path Lower Bound
- LP Heuristic
 - Dual Ascent
 - Box Step



- Branch-and-Generate Heuristic
 - Fixing on Links

DS-OPT Computational Results

Name	KS 1	KS 2	KS 3	TR	MI (I)	M (S)	WI	BN
Areas	4	2	2	1	4	1	1	1
Duty Types	3	5	3	3	4	3	3	4
Capacities	5	5	3				1	
Averages				2				
Tasks	4,345	4,345	4,345	2,867	1,317	2,436	4,453	3,014
Nodes	142.261	116.569	91.365	50.979	160.882	42.724	66.602	71.331
Arcs	1,2 Mio	2 Mio	2 Mio	851.160	3 Mio	1,8 Mio	4 Mio	977.701
Duties	114	114	117	103	87	223	252	361
Time	1 d	1 d	1 d	0,5 d	4 h	1 d	0,5 d	0,5 d

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Some Users

VS-OPT	DS-OPT		
ATC/ Terni (I)	ATC/ Terni (I)		
Athen (U) (GR)			
Berlin (D)	Berlin (D)		
Bonn (D)	Bonn (D)		
Connex (D)	Connex (D)		
DB Regio (D)	DB Regio (D)		
Geilenkirchen (D)			
	Ennepetal (D)		
Genua (I)	Genua (I)		
Mailand (U) (I)	Mailand (U) (I)		
München (S) (D)	München (S) (D)		
Norgesbus (N)	Norgesbus (N)		
Rhein-Neckar (S) (D)	Rhein-Neckar (S) (D)		
Wiesbaden (D)	Wiesbaden (D)		

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Optimization Results

	Vehicl	e Scheo	duling	Duty Scheduling			
BVG	manual	VS-OPT		manual	DS-OPT		
Bus	195	157	19,5%	n.a.	I	0,0%	
O SWB	manual	VS-OPT		manual	DS-OPT		
Bus	201	196	2,5%	280	268	4,3%	
Tram	n.a.	=	0,0%	120	117	2,5%	
VER	manual	VS-OPT		manual	DS-OPT		
Bus	n.a.	-2	n.a.	155	141	9,1%	
IESWE	manual	VS-OPT		manual	DS-OPT		
Bus	*		*	280	40	14,3%	

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ZF

Auf Sparkurs zum Ziel

Systematisierter Einsatz

Die neuen Optimierungsmethoden, die die BVG jetzt nach und nach nutzen will, stammen vom Konrad-Zuse-Zentrum für Informationstechnik und garantieren nach Roß' Angaben Einspa rungen von maximal Millionen 100Mark im Jahr. "Sie sind nötig, um unser Angebot in dieser schweren Lage stabilisieren Einsparungsdruck und dem überhaupt standhalten zu können."





WISSENSCHAFT UND PRAXIS

Rheimischer Herhur Nummer 39 : 26. September 1997 37

INFORMATIK / Ein Lehrbeispiel, wie sich Mathematik und Wirtschaft ergänzen

Auf Sparkurs zum Ziel

Das Berliner Busnetz kostet jährlich Millionen. Mit Hilfe moderner Software könnte man auf gewaltige Zuschüsse

verzichten VASCO ALEXANDER SCHMIDT

erschein sie so oft als weltab gewandte Spielerei. Doch das ist nur die Längst mischt die Praxis ein. irtschaft gespart und veroes n muß, kann sie helfen. Pro hel. Viz Grötschel, Vizepräsident Zuse-Zentrums für Infor-ik in Berlin, steht für das ewußtsein der angewand-ttik. Er ist Experte für die rische Optimierung. Seine "Wer heute die großen Vermuß sich mit Math tigen, um unnötige K

in Berlin ein Lehrheisniel. en. Die Berline be (BVG) ha en begonnen, die Einsatz r Fahrzeuge zu verbesserr

> Kosten zu decken, hat di für Jahr große Zuschüsse vom enat bekommen. Doch damit chluß; dem Land Berlin geht hus, so daß auch die BVG unter ormen Sparzwape steht. Wir enormen Sparzwang steht. "Wir i jährlich dreistellige Millionenassen janflich dreisteinge Milliöhen-eträge einsparen*, erklärt Jürgen Roß, anungsingenieur bei der BVG. "Bis im Jahr 2000 können wir von den eute rund 20 000 Mitarbeitern nur sch 15 000 barch Mitarbeitern nur

natisierter Einsatz

tum für Information ach Roß' Angaben E n maximal 100 Mil ungen von maximal 100 Millioner Mark im Jahr. "Sie sind nötig, um unse ungebot in dieser schweren Lage stabili ieren und dem Einsparungsdruch iberhaupt standhalten zu können." 1991 beauftragte die BVG d oftware-Firma IVU, ein ED m zur Betriebsplanung zu entv IVU steht für "Gesellschaft u systematisieren. sollten Linien und Fahrpläne und komfortabel am Bildschirm werden können. Außerdem man die Dienstpläne und die ine, die an den über 10 000 U-,

Stadt aushängen, auf Knopfdruck und ohne Umwege über eine Druckerei im eigenen Haus produzieren. Nach und nach wurden diese Werkzeuge einge-führt. Das jetzt installierte Optimie-rungsmodul für die Umlaufplanung von Straßenbahnen und Bussen ist der bisrund 1800 BVG-Busse morgens sein De-pot verläßt und nach Dienstschluß dort wieder landet. Es gibt Eindecker, Doppeldecker, Ge-lenk- und Minibusse, aber nicht jeder typ kann jede Route bedienen. Au-dem sind komplizierte betriebliche p kann jede Roue Sculetcher m sind komplizierte betriebliche echtliche Bedingungen zu beach-twa Pausenregelungen. Ziel ist es

en, daß die Ar Komfortable Hilfe ausgenutzt wird und die Leerfahrte won einem Einsatzort zum nächste möglichst kurz sind. Alle diese Zielvo ort zum nächster Zwar werden in Deutsch Verkehrsplanung meist schon Compu-ter eingesetzt; diese aber unterstützen die Planer oft nur als ein einfaches, wenn auch komfortables Hilfsmittel. Andere Verkehrsunternehmen, etwa die he Struktur. Hamburger Hochbahn AG, setzen Com puter schon seit Ende der siebziger Jah illen Fragen nach optimalen Mischver nältnissen, bei Güterflüssen in einer Fr brik und auch bei Stundenpläne lich gesprochen b m Vieleck in der Ebene und e aden, die durch das Vieleck verli Nun verschiebt man die Gerade nach rechts. Ziel Ist es, den letzten Punkt der Vielecks zu bestimmen, den die Gerade steneinsparung nicht nur annä-rnd, sondern ganz exakt. Ein wissenlicher Durchbruch. mathematische Grundlage ihre bildet eine komplexes Glei chungssystem, eine sogenannte Matrix, mit mehr als 100 000 Zeilen und 70 Milpte Lösung des Optimierung ms. Das Vieleck bei den Bus-Um

nehr als 100 000 Zehlen in der gigan-ten Spalten. Die Zahlen in der giganplänen ist sehr viel komplexer, mar tischen Tabelle geben an, wie die E Kristall mit mehreren Billionen Ecker sis file die 11e

chen läßt. Und genau diese Eig det er für diesen kleinen Teil eine Li sung, so vergrößert er nach und nach das Problem, bis er eine Lösung für die

zeß gera

on der Mathematik snüren die I

Die Politik freilich erwartet zur Zeit

nur die größtmögliche Einsparung der Mathematik hat sie dafür ein



Artikel erschienen am 26. Sep 1997

The Psychology of Improvement

- Company goals
- Manager goals
- Dispatcher goals

The 15% rule



IP Model for Integrated Scheduling

$$\min \sum_{d \in D} \sum_{ij \in A^d} c_{ij}^d x_{ij}^d + \sum_{j \in J} c_j y_j$$

$$\sum_{d \in D} \sum_{ij \in A^d} x_{ij}^d = 1 \quad \forall t \in T \quad (\text{Trips})$$

$$\sum_{ij \in A^d} x_{ij}^d - \sum_{it \in A^d} x_{it}^d = 0 \quad \forall t \in T, d \in D \quad (\text{V-Flow})$$

$$\sum_{d \in A^d} x_{dt}^d \leq \kappa_d \quad \forall d \in D \quad (\text{V-Cap})$$

$$\sum_{j \in J} a_{ij} y_j = 1 \quad \forall i \in t \in T \quad (\text{Tasks})$$

$$\sum_{d \in D} \sum_{ij \in A^d} x_{ij}^d - \sum_{j \in J} a_{ij} y_j = 0 \quad \forall i \in t \in H \quad (\text{Coupling})$$

$$x_{it}^d, y_j \in \{0,1\} \quad (\text{Integrality})$$

$$= \text{T-Timetabled Trips} \quad D-\text{Depots}$$

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IS-OPT

- Lagrangean Relaxation on Coupling Constraints
 - Proximal Bundle Method
 - Approximate Solution of Vehicle and Duty Scheduling Components
- Branch-and-Generate Heuristic
 - Fixing Deadhead Trips



Trassenbörse = track auctioning

European Union:

History of our project

- Establish a rail traffic market
- open the market to competition
- Deregulate/Regulate this market









Trassenbörse = track auctioning

What is the goal of the deregulation attempts? General answer: More traffic at lower cost, better service

How do you measure?

Our answer: in terms of willingness to pay (Zahlungsbereitschaft)

What is the "good" of this market?

Our answer: Fahrplantrasse

- = timetabled dedicated track section
- = use of railway infrastructure in time and space
- = brief: "timetabled track"

Public Transportation Summary

- Possible savings in public transport
- Can public transport break even?
- Where are the bottlenecks?
- What can OR do?
- Multi-modality considerations
- individual vs. public transport?



 What is a "good" transportation system? (HARD question)

Contents

- 1. Introduction
 - Where am I from?
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- 2. What is OR? (A name is a name, or not?)
- 3. OR on OR
- 4. Answering the HARD questions
 - What can we do? Examples of Success Stories:
 - Linear and integer programming
 - Public transportation
 - Telecommunication
 - What should we look at?
- 5. What is good OR?

Martin Grötsche

ZI B Telecom Team

The Telecom Group

Andreas Bley Andreas Eisenblätter Martin Grötschel Thorsten Koch Arie Koster Roland Wessäly Adrian Zymolka Associates

Manfred Brandt Sven Krumke Frank Lutz Diana Poensgen Jörg Rambau

Clyde Monma (BellCore, ...) Mechthild Opperud (ZIB, Telenor) Dimitris Alevras (ZIB, IBM) Christoph Helmberg (Chemnitz)

Martin Grötsche

ZIB Partners from Industry

Bell Communications Research Telenor (Norwegian Telecom) E-Plus (acquired by KPN in 01/2002) **DFN-Verein** Bosch Telekom (bought by ?) Siemens Austria Telekom (Italia Telecom?) T-Systems Nova (T-Systems, Deutsche Telekom) **KPN Telecel-Vodafone**

Atesio (ZIB spin-off company)



What is the Telecom Problem?

Speech

Video

Etc.

Data

Design excellent technical devices and a robust network that survives all kinds of failures and organize the traffic such that high quality telecommunication between very many individual units at many locations is feasible at low cost!



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What is the Telecom Problem?

Design excellent technical devices and a robust network that survives all kinds of failures and organize the traffic such that high quality telecommunication between very many individual units at many locations is feasible at low cost!

This problem is too general to be solved in one step.

Approach in Practice:

- Decompose whenever possible
- Look at a hierarchy of problems
- Address the individual problems one by one
- Recompose to find a good global solution

Cell Phones, Mathematics, and OR



Designing mobile phones

- Task partitioning
- Chip design (VLSI)
- Component design

- Computational logic
- Combinatorial optimization
- Differential algebraic equations

Producing Mobile Phones

- Production facility layout
- Control of robots
- Lot sizing
- Scheduling
- Logistics

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- Linear and integer programming
- Combinatorial optimization
- Control of CNC machines
 Ordinary differential equations

Marketing and Distributing Mobiles

- Financial mathematics
- Transportation optimization

Design and Production of I Cs and PCBs



Integrated Circuit (IC)



Printed Circuit Board (PCB)



Problems: Logic Design, Physical Design Correctness, Simulation, Placement of Components, Routing, Drilling,...



Siemens Problem

printed circuit board da4







after

Network Design: Tasks to be solved Some Examples

- Locating the sites for antennas (TRXs) and base transceiver stations (BTSs)
- Assignment of frequencies to antennas
- Cryptography and error correcting encoding for wireless communication
- Clustering BTSs
- Locating base station controllers (BSCs)
- Connecting BTSs to BSCs



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Network Design: Tasks to be solved Some Examples (continued)

- Locating Mobile Switching Centers (MSCs)
- Clustering BSCs and Connecting BSCs to MSCs
- Designing the BSC network (BSS) and the MSC network (NSS or core network)
 - Topology of the network
 - Capacity of the links and components
 - Routing of the demand
 - Survivability in failure situations

Most of these problems turn out to be Combinatorial Optimization or Mixed Integer Programming Problems



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Connecting Mobiles: What's up?





Frequency Planning Problem

Find an assignment of frequencies to transmitters that satisfies

- all separation constraints
- all blocked channels requirements

and either

- avoids interference at all
- or
- minimizes the (total/maximum) interference level


Minimum Interference Frequency Assignment Problem

Integer Linear Program:

 $\min \sum_{vw \in E^{co}} c_{vw}^{co} z_{vw}^{co} + \sum_{vw \in E^{ad}} c_{vw}^{ad} z_{vw}^{ad}$ $s.t. \sum_{f \in F_v} x_{vf} = 1$ $x_{vf} + x_{wg} \leq 1$ $x_{vf} + x_{wf} \leq 1 + z_{vw}^{co}$ $x_{vf} + x_{wg} \leq 1 + z_{vw}^{ad}$ $x_{vf} + x_{wg} \leq 1 + z_{vw}^{ad}$ $x_{vf} + x_{wg} \leq 1 + z_{vw}^{ad}$ $x_{vf} + z_{vw} \leq 1 + z_{vw}^{ad}$

 $\forall v \in V$

 $\forall vw \in E^{d}, |f - g| < d(vw)$ $\forall vw \in E^{co}, f \in F_{v} \cap F_{w}$ $\forall vw \in E^{ad}, |f - g| = 1$



Region Berlin - Dresden



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The UMTS Radio Interface

Completely new story



Network Optimization



What needs to be planned?

- Topology
- Capacities
- Routing
- Failure Handling (Survivability)
- IP Routing
- Node Equipment Planning
- Optimizing Optical Links and Switches

DISCNET: A Network Planning Tool (Dimensioning Survivable Capacitated NETworks) Atesio ZIB Spin Off

Grötsche

The Network Design Problem

Communication Demands





Mathematical Model

$$\begin{split} \min \sum_{e \in E} \sum_{i=1}^{T_e} k_e^i x_e^i & \checkmark \text{ topology decisison} \\ & \checkmark \text{ capacity decisions} \\ & \checkmark \text{ normal operation routing} \\ & x_e^{t-1} \ge x_e^t \quad e \in E, t = 1, \dots, T_e \\ & \checkmark \text{ component failure routing} \\ & y_e = \sum_{i=0}^{T_e} c_e^i x_e^i \quad e \in E \\ & y_e \ge \sum_{m \in D} \sum_{i \in \mathbb{N}^n_e \in \mathbb{N}^n} f_m^0(P) \quad e \in E \\ & y_e \ge \sum_{m \in D} \sum_{i \in \mathbb{N}^n_e \in \mathbb{N}^n_e} f_m^0(P) \quad e \in E \\ & d_{av} = \sum_{P \in \mathbb{P}^n_m} f_m^0(P) \quad uv \in D \\ & f_{av}^*(P) \ge 0 \qquad s \in S, uv \in D_s, P \in \mathbb{P}^s_m \end{split}$$

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ZH

Flow chart

LP-relaxation

LP-based approach:

Polyhedral combinatorics Valid inequalities (facets) Separation algorithms Heuristics Feasibility of a capacity vector



Finding a Feasible Solution?

Heuristics

. . .

- Local search
- Simulated Annealing
- Genetic algorithms

Manipulation of

- Routings
- Topology
- Capacities

Problem Sizes

Nodes	Edges	Demands	Routing-Paths
15	46	78	> 150 x 10e6
36	107	79	> 500 x 10e9
36	123	123	> 2 x 10e12



How much to save?

Real scenario

- 163 nodes
- 227 edges
- 561 demands

PhD Thesis:

wessaely@atesio.de

34% potential savings! == > hundred million dollars



Summary

Telecommunication Problems such as

- Frequency Assignment
- Locating the Nodes of a Network Optimally
- Balancing the Load of Signaling Transfer Points
- Integrated Topology, Capacity, and Routing Optimization as well as Survivability Planning
- Planning IP Networks
- Optical Network Design
- and many others

can be succesfully attacked with optimization techniques.

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5.

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- 4. Answering the HARD questions
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 - What should we look at?
 - What is good OR?

Summary Telecommunication

The OR approach

- Helps understanding the problems arising
- Makes much faster and more reliable planning possible
- Allows considering variations and scenario analysis
- Allows the comparision of different technologies
- Yields feasible solutions
- Produces much cheaper solutions than traditional planning techniques
- Helps evaluating the quality of a network.



There is still a lot to be done, e.g., for the really important problems, optimal solutions are way out of reach!

The OR Challenges

- Finding the right ballance between flexibility and controlability of future networks
- Controlling such a flexible network
- Handling the huge complexity
- Integrating new services easily
- Guaranteeing quality
- Finding appropriate Mathematical Models
- Finding appropriate solution techniques (exact, approximate, interactive, quality guaranteed)

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The Network Business will Change

Courtesy Dr. Winter (E-Plus)



Integrating Variable Multimedia Services

Courtesy Dr. Winter (E-Plus)



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The OR Challenges

What is a good telecommunication network?



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5. What is good OR?

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What is good OR?

Staying in touch with everybody





Challenges

- first line of the text outlining the conference theme:
 "One of the most important concerns of the European Union is the ensuring and continuous improvement of goods and services within the Europe of today and tomorrow."
- We (the OR community) have not given enough thought so far to what we mean by "improvement of goods and services".



Challenging Questions

- What is a GOOD public transportation system?
 Directly related to the conference theme:
- What is a GOOD telecommunication system?
 Even more directly referring to the conference theme:
- Is the Internet really beneficial?
 For whom? Under what rules?....



Directions

I am myself a person preferring to address questions

- that can be quantified precisely
- that have clean data and
- that have clear objectives and
- that can be modeled nicely.
- However, I think we should start addressing problems seriously
- that can't be quantified precisely
- that don't have clean data and
- that don't have clear objectives and
- that can't be modeled nicely.
- but that are of higher political and social relevance

Gröteche

Directions

OR has the potential – employing its interdisciplinary strength – to contribute to other issues such as:

- unemployment
- fair trade
- safe water supply
- energy supply, in particular renewable energy
- electronic services (not only their management)



Directions

- P. Hansen, "A short discussion of the OR crisis" European Journal of Operational Research 38(1989)277-281
 - "No general agreement seems to have been reached about its methodology, and the directions in which it should evolve. ... There are many ways to live a life of OR, to discover new results and apply them, and thus to enjoy OR's truth and beauty."
- R. Burkard, "OR Utopia" European Journal of Operational Research 119(1999)224-234

"The borders of OR Utopia have yet another quality: people can come and go, without passport. There is no quota for foreigners... OR Utopia...is a peaceful border between OR, mathematics, and computer science, ...management science, economy, logistics, ..."



Science in the View of the Public

- I am concerned since I see downfalls of scientific fields such as nuclear technology that has made many promises and brought fear.
- The same is presently happening to biotechnology (many people are simply afraid of the progress announced).
- Similar tendencies are currently coming up in nano technology.

OR in the View of the Public

- OR has to watch out that it keeps the right balance and people do not start getting afraid of OR.
- I see tendencies in public talks of company bosses, politicians, journalists, and union leaders that optimization means nothing but eliminating jobs, cutting down services, etc.





my advice

- Don't care about definitions of OR
- Let us not define the field OR, let us just be OR (OR stands for itself, no interpretation)
- Be flexible with your goals and approaches
- Enjoy the stuff that you do
- Position yourself depending on your own needs, goals, and wishes and that of your company or academic institution



OR is a transdisciplinary discipline

my advice

Try to contribute to

- science
- society
- business
- with the tools that you have, respecting the work and contributions of others, at your best possible level.



Or on OR The End

Martin Grötschel

20th European Conference on Operational Research EURO XX, Rhodes, Greece July 7, 2004



Institute of Mathematics, Technische Universität Berlin (TUB)

DFG-Research Center "Mathematics for key technologies" (FZT 86)

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